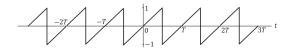
TIFR- 2017

1. Denote the commutator of two matrices A and B by [A,B]=AB-BA and the anti-commutator by $\{A,B\}=AB+BA$.

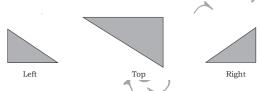
If $\{A, B\} = 0$, we can write [A, BC] =

- (a). -B[A, C]
- (b). $B\{A, C\}$
- (c). $-B\{A,C\}$
- (d). [A, C]B
- 2. Consider the waveform $\boldsymbol{x}(t)$ shown in the diagram below.

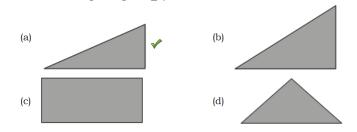


The Fourier series for x(t) which gives the closes approximation to this waveform is

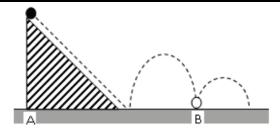
- (a). $x(t) = \frac{2}{\pi} \left[\cos \frac{\pi t}{T} \frac{1}{2} \cos \frac{4\pi t}{T} + \frac{1}{3} \cos \frac{3\pi t}{T} + \cdots \right]$
- (b). $x(t) = \frac{2}{\pi} \left[-\sin\frac{\pi t}{T} + \frac{1}{2}\sin\frac{2\pi t}{T} \frac{1}{3}\sin\frac{3\pi t}{T} + \cdots \right]$
- (c). $x(t) = \frac{2}{\pi} \left[\sin \frac{\pi t}{T} \frac{1}{2} \sin \frac{2\pi t}{T} + \frac{1}{3} \sin \frac{3\pi t}{T} + \cdots \right]$
- (d). $x(t) = \frac{2}{\pi} \left[-\cos\frac{2\pi t}{T} + \frac{1}{2}\cos\frac{4\pi t}{T} \frac{1}{3}\cos\frac{6\pi t}{T} + \frac{1}{3}\cos\frac{6\pi t}{T} \right]$
- 3. A solid tetrahedron (solid with four plane sides) has the following projections (drawn to scale) when seen from three different sides:



When viewed from the front, its projection will be

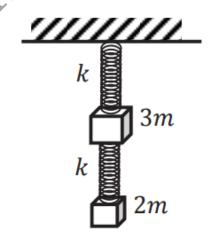


4. A small elastic ball of mass m is placed at the apex of a 45° inclined plane as shown in the figure below.



The ball is allowed to slip without friction down the plane (along the dotted line), hit the ground (as shown) and bounce along it. If the height of the inclined plane is h and the coefficient of restitution between the ball and the ground is 0.5, then the distance AB, as marked on the figure, will be

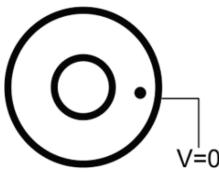
- (a). 3h
- (b). 2h
- (c). $(1+\sqrt{2})h$
- (d). $3\sqrt{2}h$
- 5. Two masses 3m and 2m are suspended vertically by identical massless springs, each of stiffness constant k. The mass 2m is suspended from the mass 3m and the mass 3m is suspended from a rigid support, as shown in the figure. If only vertical motion is permitted, the frequencies of small oscillations of this system are

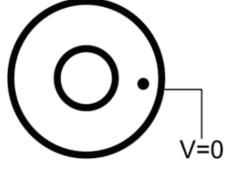


- (a). $\sqrt{\frac{k}{m}}$, $\sqrt{\frac{k}{6m}}$
- (b). $\sqrt{\frac{k}{2m}}$, $\sqrt{\frac{k}{3m}}$
- (c). $\sqrt{\frac{k}{m}}$, $\sqrt{\frac{3k}{2m}}$
- (d). $\sqrt{\frac{2k}{3m}}$, $\sqrt{\frac{3k}{2m}}$
- 6. Two long hollow conducting cylinders, each of height h, are placed concentrically on the ground, as shown in the figure (top view). The outer cylinder is grounded, while the inner cylinder is insulated. A

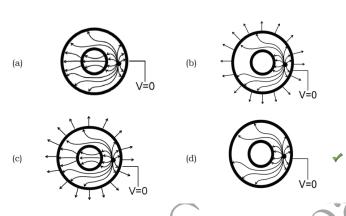
positive charge (the black dot in the figure) is placed between the cylinders at a height h/2 from the ground.

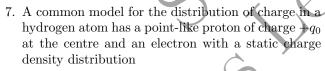
If the resistance of the loop is R, the torque τ required to prevent the loop from rotating will be





Which of the following figures gives the most accurate representation (top view) of the lines of force?





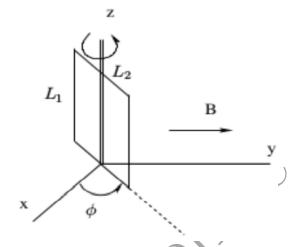
$$\rho(r) = -\frac{q_0}{\pi a^3} e^{-2r/a}$$

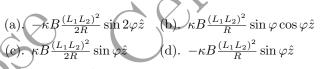
where a is a constant. The electric field \vec{E} at r=adue to this system of charges will be

(a).
$$-\frac{5q_0}{4\pi\epsilon_0 e^2 a^2} \hat{r}$$
 (b). $-\frac{5q_0}{4\pi\epsilon_0 e^2 a^2} \hat{r}$ (c). $\frac{5q_0}{4\pi\epsilon_0 e^2 a^2} \hat{r}$ (d). $\frac{3q_0}{4\pi\epsilon_0 e^2 a^2} \hat{r}$

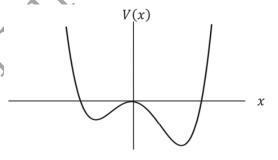
8. A rectangular metallic loop with sides L_1 and L_2 is placed in the vertical plane, making an angle φ with respect to the x-axis, as shown in the figure, and a spatially uniform magnetic field $\vec{B} = B\hat{y}$ is applied. The loop is free to rotate about the \hat{z} -axis (shown in the figure with a double line). The magnetic field changes with time at a constant rate

$$\frac{dB}{dt} = \kappa$$

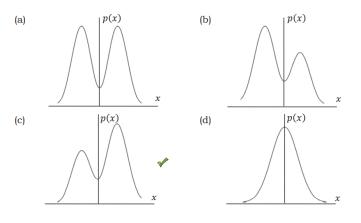




Consider the 1-D asymmetric double-well potential V(x) as sketched below.



The probability distribution p(x) of a particle in the ground state of this potential is best represented by



10. The normalized wave function of a particle can be

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written as

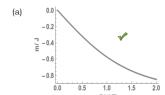
$$\Psi(x) = N \sum_{n=0}^{\infty} \left(\frac{1}{\sqrt{7}}\right)^n \varphi_n(x)$$

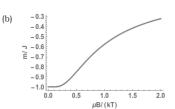
where $\varphi_n(x)$ are the normalized energy eigenfunctions of a given Hamiltonian. The value of N is

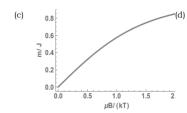
- (a). $\sqrt{1/7}$
- (b). $\sqrt{6/7}$
- (c). $\sqrt{3/7}$
- (d). $\sqrt{(6-2\sqrt{7})/7}$
- 11. Consider a system of non-interacting particles with integer angular momentum J at a temperature T. This system is placed in a magnetic field B in the z direction. The energy of a state with $J_z = m\hbar$ is

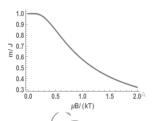
$$E_m = m\mu_B B$$

with $\mu_B > 0$. The fractional magnetization of the particles as a function of $\mu_B B/k_B T$ can be represented as



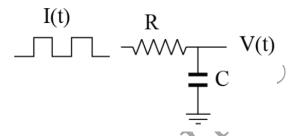




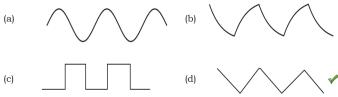


- 12. The separation between neighbouring absorption lines in a pure rotational spectrum of the hydrogen bromide (HBr) molecule is 2.23 meV. If this molecule is considered as a rigid rotor and the atomic mass number of Br is 80, the corresponding absorption line separation in deuterium bromide (DBr) molecule, in units of meV, would be
 - (a). 2.234
 - (b). 1.115
 - (c). 1.128
 - (d). 4.461
- 13. Consider a 2-D square lattice. The ratio of the kinetic energy of a free electron at a corner of the first Brillouin zone (E_c) to that of an electron at the midpoint of a side face of the same zone (E_m) is $E_c/E_m =$

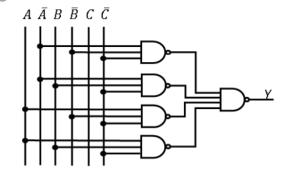
- (a). 1/2
- (b). 2
- (c). $\sqrt{2}$
- (d). 1
- 14. A current source produces a square wave I(t) of 1.0 V peak-to-peak voltage and is used to drive the RC circuit shown below.



Which of the following represents the correct voltage across the capacitor C?



15. The output (Y) of the following circuit will be



- (a). $\bar{A} + B + \bar{C}$
- (b). \bar{A}
- (c). \bar{B}
- (d). \bar{C}
- 16. The matrix

$$\begin{pmatrix} 100\sqrt{2} & x & 0 \\ -x & 0 & -x \\ 0 & x & 100\sqrt{2} \end{pmatrix}$$

where x > 0, is known to have two equal eigenvalues. Find the value of x.

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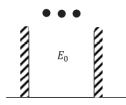
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- 17. A space telescope in orbit around the Earth discovers a new planet, which is observed to move around the Sun by an angle of 4.72 milliradians in a year. Assuming a circular orbit, estimate the distance, in A.U., of the planet from the Sun.
- 18. A system of particles occupying single-particle levels and obeying Maxwell-Boltzmann statistics is in thermal equilibrium with a heat reservoir at temperature T. If the population distribution in the non-degenerate energy levels is as shown in the table below, what would be the temperature of the system in degree Kelvin?

Energy (eV)	Population %
30.30	3.16
21.60	8.69
13.01	23.54
4.31	64.61

- 19. A thermally isolated container stores N_2 gas at $27.24^{\circ}C$ at one atmospheric pressure. Suddenly the pressure of the gas is increased to two atmospheric pressures. Assuming N_2 to behave as an ideal gas, estimate the change in temperature of the gas, in Celsius degrees (${}^{\circ}C$).
- 20. A beam of plane microwaves of wavelength 12 cm strikes the surface of a dielectric at 45°. If the refractive index of the dielectric is 4/3, what will be the wavelength, in units of mm, of the microwaves inside the dielectric?
- 21. A quantum mechanical system consists of a onedimensional infinite box, as indicated in the figures below.





- 3 (three) identical non-interacting spin- $\frac{1}{2}$ particles, are first placed in the box, and the ground state energy of the system is found to be $E_0 = 18$ eV. If 7 (seven) such identical particles are placed in the box, what will be the ground state energy, in units of eV?
- 22. The energy of an electron in the ground state of the He atom is -79 eV. Considering the Bohr model of the atom, what would be 10 times the first ionization potential for a He⁺ ion, in units of eV?
- 23. Cosmic ray muons, which decay spontaneously with proper lifetime 2.2 μ s, are produced in the atmosphere, at a height of 5 km above sea level. These

move straight downwards at 98% of the speed of light.

Find the percent ratio $100 \times (N_A/N_B)$ of the number of muons measured at the top of two mountains A and B, which are at heights 4,848 m and 2,682 m respectively above mean sea level.

- 24. A signal is to be sent from a coaxial cable with impedance 40Ω into a second coaxial cable with impedance 60Ω . We can prevent reflection at the joint between the cables, by adding an impedance in parallel to the second cable. What should be the value, in units of Ohms (Ω) , of that impedance?
- 25. An AC voltage source has an internal resistance of $50~\Omega$ and is specified to deliver an rms voltage of 50~V to a matched load. If you connect this AC source to a cathode-ray oscilloscope with $1~M\Omega$ input setting, what will be the peak-to-peak voltage you observe?
- 26. A unitary matrix U is expanded in terms of a Hermitian matrix H, such that

$$U=e^{i\pi H/2}$$

If we know that

$$H = \begin{pmatrix} 1/2 & 0 & \sqrt{3}/2 \\ 0 & 1 & 0 \\ \sqrt{3}/2 & 0 & -1/2 \end{pmatrix}$$

then U must be

(a).
$$\begin{pmatrix} i & 1/2 & \sqrt{3}/2 \\ 1/2 & i & 1/2 \\ \sqrt{3}/2 & 1/2 & i \end{pmatrix}$$
 (b). $\begin{pmatrix} i/2 & 0 & i\sqrt{3}/2 \\ 0 & i & 0 \\ i\sqrt{3}/2 & 0 & -i/2 \end{pmatrix}$

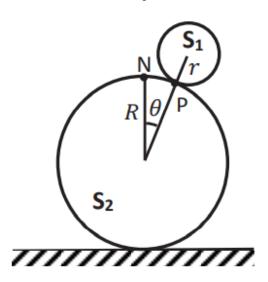
(c).
$$\begin{pmatrix} 1 & 0 & \sqrt{3} \\ 0 & 2 & 0 \\ \sqrt{3} & 0 & -1 \end{pmatrix}$$
 (d). $\begin{pmatrix} 2i & 1 & \sqrt{3}/2 \\ 1 & 2i & 0 \\ \sqrt{3}/2 & 0 & 2i \end{pmatrix}$

- 27. A liquid is flowing through a capillary tube of inner radius r under the influence of an external pressure P. The uncertainties in the measurements of P and r are found to be 2% and 1%, respectively. The uncertainty in the flow of liquid per second is
 - (a). 4.47%
 - (b). 2.23\%
 - (c). 2.83%
 - (d). 3.61%
- 28. A uniform solid sphere S_1 of radius r and mass m is rolling without slipping on top of another sphere S_2 of radius R, as shown in the figure. Initially, S_1 was at rest directly on top of S_2 , and then it started rolling down under the influence of gravity. The

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point of contact P subtends an instantaneous angle θ from the topmost point N of the lower sphere at the centre of the lower sphere.



At what minimum value of θ will the spheres lose contact?

- (a). $\cos^{-1} \frac{5}{12}$
- (b). $\cos^{-1} \frac{5}{13}$
- (c). $\cos^{-1} \frac{2}{3}$
- (d). $\cos^{-1} \frac{12}{12}$
- 29. An electromagnetic wave in free space is described

$$\vec{E}(x, y, z, t) = \hat{z}E_0 \cos \frac{1}{2}(kx - \sqrt{3}ky - 2\omega t)$$

The Poynting vector associated with this wave is along the direction

- (a). $\hat{x} + \sqrt{3}\hat{y}$
- (c). $-\sqrt{3}\hat{x} + \hat{y}$
- 30. Electrons in a given system of hydrogen atoms are described by the wave function

$$\psi(r,\theta,\varphi) = 0.8\Psi_{100} + 0.6e^{i\pi/3}\Psi_{311}$$

where the $\Psi_{n\ell m}$ denote normalized energy eigenstates. If $(\hat{L}_x, \hat{L}_y, \hat{L}_z)$ are the components of he orbital angular momentum operator, the expectation value of \hat{L}_x^2 in this system is

- (a). $1.5\hbar^2$
- (b). $0.36\hbar^2$
- (c). $0.18\hbar^2$
- (d). Zero

31. In two dimensions, two metals A and B, have the number density of free electrons in the ratio

$$n_A: n_B = 1:2$$

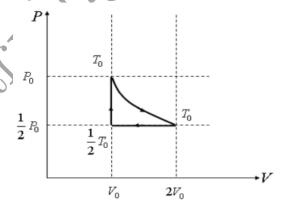
The ratio of their Fermi energies is

- (a). 2:3
- (b). 1:2
- (c). 1:4
- (d). 1:8
- 32. One mole of monoatomic ideal gas is initially at pressure P_0 and volume V_0 .

The gas then undergoes a three-stage cycle consisting of the following processes:

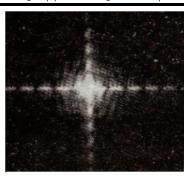
- i) An isothermal expansion till it reaches volume $2V_0$, and heat Q flows into the gas
- ii) An isobaric compression back to the original volume V_0
- iii) An isochoric increase in pressure till the original pressure P_0 is regained.

The efficiency of this cycle can be expressed as



- (b). $\epsilon = \frac{4Q + 2RT_0}{4Q 3RT_0}$
- (a). $\epsilon = \frac{4Q + 2RT_0}{4Q + RT_0}$ (c). $\epsilon = \frac{4Q 2RT_0}{4Q + RT_0}$
- (d). $\epsilon = \frac{4Q 2RT_0}{4Q + 3RT_0}$
- 33. A deuteron of mass M and binding energy B is struck by a gamma ray photon of energy E_{γ} , and is observed to disintegrate into a neutron and a proton. If $B \ll Mc^2$, the minimum value of E_{γ} must
- (a). $2B + \frac{B^2}{2Mc^2}$ (b). $B + \frac{B^2}{Mc^2}$ (c). $\frac{1}{2} \left(3B + \frac{B^2}{Mc^2}\right)$ (d). $\frac{1}{2} \left(2B + \frac{B^2}{Mc^2}\right)$
- 34. Light passes through a narrow slit and gives the Fraunhofer diffraction pattern shown in the adjacent figure.

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of the same equilibrium radius?

You may use the following data:

38. Consider the following situations.

Ans = 0.7

Liquid	Density in gm cm ⁻³	Surface tension in N m ⁻¹		
water	1.0	0.073		
mercury	13.6	0.487		

What would be the numerical value of the ratio $\nu_{\rm Hg}/\nu_{\rm H2\,O}$ of the frequencies of oscillation between a drop of mercury (Hg) and a drop of water (H2 O)

Which of the following could be the shape of the slit?



(c)









- 35. For exact calculation and minimum complexity, two four-digit binary numbers can be added with
 - (a). 1 full adder and 3 half-adders
- (b). 2 full adders and 2 half-adders
- (c). 3 full adders and 1 half-adder
- (d). 4 full adders
- 36. Evaluate the expression

$$n! \int_0^A dx_{n-1} \int_0^{x_{n-1}} dx_{n-2} \int_0^{x_{n-2}} dx_{n-3} \cdots \int_0^{x_3} dx_2 \int_0^x dx_2 \int_0^x$$

37. In outer space, where the effects of gravity can be neglected, a drop of liquid assumes a spherical shape. However, when disturbed it undergoes shape oscillations (see figure). The frequency ν of oscillation of a drop depends on its equilibrium radius, its density and the surface tension.



- In situation A, two semi-infinite earthed conducting planes meet at right-angles. A point charge q, is placed at a distance d from each plane, as shown in the figure A. The magnitude of the force exerted on the charge q is denoted F_A .
- In situation B, the same charge q is kept at the $dx_1^{x_1}$ distance d from an infinite earthed conducting plane, as shown in the figure B. The magnitude of the force exerted on the charge q is denoted F_B .

Find the numerical ratio F_A/F_B

39. Two identical bosons may occupy any of two energy levels $0, \varepsilon$, where $\varepsilon > 0$. The lowest energy state is doubly-degenerate and the excited state is non-degenerate. Assume that the two-particle system is in thermal equilibrium at a temperature T. Calculate the average energy $\langle E \rangle$. What will be the leading term of

$$\frac{\langle E \rangle}{\exp\left(-\frac{\varepsilon}{k_B T}\right)}$$

at low temperature?

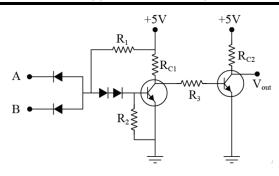
40. Which digital logic gate is mimicked by the following silicon diode and silicon transistor circuit?

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Ans = AND or (A.B)

41. The value of the integral

$$\int_0^\infty \frac{dx}{x^4 + 4}$$

Is

- (a). π
- (b). $\frac{\pi}{2}$
- (c). $\frac{\pi}{4}$
- (d). $\frac{\pi}{9}$
- 42. The Lagrangian of a system described by a single generalised coordinate q is

$$L = \frac{1}{2}\dot{q}\sin^2q$$

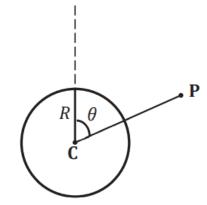
Its Hamiltonian is

- (a). not defined
- (c). $-\dot{q}\sin^2 q$
- 43. A one-dimensional quantum harmonic oscillator of natural frequency ω is in thermal equilibrium with a heat bath at temperature T. The mean value $\langle E \rangle$ of the energy of the oscillator can be written as

- 44. Consider a spherical shell with radius R such that the potential on the surface of the shell in spherical coordinates is given by,

$$V(r = R, \theta, \varphi) = V_0 \cos^2 \theta$$

where the angle θ is shown in the figure. There are no charges except for those on the shell. The potential outside the shell at the point P a distance 2R away from its center C (see figure) is



- 45. A quantum mechanical system which has stationary states $|1\rangle$, $|2\rangle$ and $|3\rangle$, corresponding to energy levels 0 eV, 1 eV and 2 eV respectively, is perturbed by a potential of the form

$$\hat{V} = \varepsilon |1\rangle\langle 3| + \varepsilon |3\rangle\langle 1|$$

where, in eV, $0 < \varepsilon \ll 1$.

The new ground state, correct to order ε , is approximately.

- (a). $(1 \frac{\varepsilon}{2})|1\rangle + \frac{\varepsilon}{2}|3\rangle$ (b). $|1\rangle + \frac{\varepsilon}{2}|2\rangle \varepsilon|3\rangle$ (c). $|1\rangle + \frac{\varepsilon}{2}|3\rangle$ (d). $|1\rangle \frac{\varepsilon}{2}|3\rangle$

- 46. Hydrogen atoms in the atmosphere of a star are in thermal equilibrium, with an average kinetic energy of 1 eV. The ratio of the number of hydrogen atoms in the 2nd excited state (n = 3) to the number in the ground state (n = 1) is
 - (a). 3.16×10^{-11}
- (b). 1.33×10^{-8}
- (c). 3.16×10^{-8}
- (d). 5.62×10^{-6}

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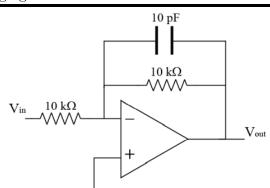
47. A photomultiplier tube is used to detect identical light pulses each of which consists of a fixed number of photons. The photoelectric efficiency is 10%, i.e. a photon has 10% probability of causing the emission of a detectable photoelectron. The photomultiplier gain is 10^6 .

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 $I_{
m max}$

20 ns

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The typical output current, as a function of time, is shown by the figure below for a few pulses, where $I_{\rm max}$ is 80 μ A. It follows that the number of photons in each pulse is

(a). 5×10^6

I(t)

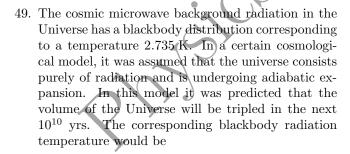
(b). 5

- (c). 800
- (d). 50
- 48. A subatomic particle ψ and its excited state ψ^* have rest masses 3.1 GeV/ c^2 and 3.7 GeV/ c^2 respectively. A table of its assigned quantum numbers is given below.

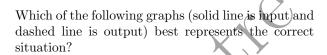
Angular Momentum	Parity	C-Parity	Isospin	Electric charge
I = 1	P = -1	C = -1	I = 0	O = 0

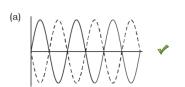
If π^{0*} is an excited state of π^0 with a mass of about 1.3 GeV/ c^2 , which of the following reactions is possible when the above quantum numbers are conserved?

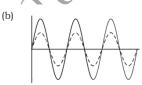
- (a). $\psi^* \to \gamma \gamma$
- b). $\psi^* \to \psi \pi^+ \pi$
- (c). $\psi^* \to \pi^0 \pi^0$
- (d). $\psi^* \rightarrow \psi \pi^{0*}$

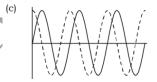


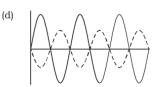
- (a). 0.9116 K
- (b). 2.078 K
- (c). 1.896 K
- (d). 1.526 K
- 50. The following circuit is fed with an input sine wave of frequency 50 Hz.











51. Write down x(t), where x(t) is the solution of the following differential equation

$$\left(\frac{d}{dt} + 2\right) \left(\frac{d}{dt} + 1\right) x = 1,$$

with the boundary conditions

$$\frac{dx}{dt}\Big|_{t=0} = 0, x(t)|_{t=0} = -\frac{1}{2}$$

52. A particle of mass m, confined to one dimension x, is in the ground state of a harmonic oscillator potential with a normalized wave function

$$\Psi_0(x) = \left(\frac{2a}{\pi}\right)^{\frac{1}{4}} e^{-ax^2}$$

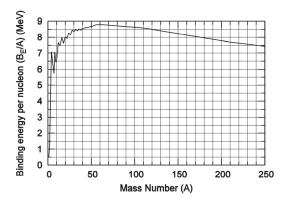
where $a = m\omega/2\hbar$. Find the expectation value of x^8 in terms of the parameter a.

53. Electrons in a metal are scattered by both impurities and phonons. The impurity scattering time is 8×10^{-12} s and the phonon scattering time is 2×10^{-12} s. Taking the density of electrons to be 3×10^{14} m⁻³, find the conductivity of the metal in units of A V⁻¹ m⁻¹. [Assume that the effective mass of the electrons is the same as that of a free electron.]

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54. In a theoretical model of the nucleus, the binding energy per nucleon was predicted as shown in the figure below.



If a nucleus of mass number A=240 undergoes a symmetric fission to two daughter nuclei each of mass number A=120, write down the amount of energy released in this process, in units of MeV, using this theoretical model.

55. Assume that the crystal structure of metallic copper (Cu) results in a density of atoms $\rho_{\text{Cu}} = 8.46 \times 10^{28} \text{ m}^{-3}$. Each Cu atom in the crystal donates one electron to the conduction band, which leads, for the 3-D Fermi gas, to a density of states

$$g(\varepsilon) = \frac{1}{2\pi^2} \left(\frac{2m^*}{\hbar^2}\right)^{3/2} \varepsilon^{1/2}$$

where m^* is the effective mass of the conduction electrons. In the low temperature limit (i.e. T=0 K), find the Fermi energy E_F , in units of eV. You may assume m^* to be equal to the free electron mass m_e .

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53

54

55

 13.5×10^{-6}

240

6.87